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# EMPOWERING THE USE OF VARIANT TABLES IN MASS CUSTOMIZATION

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Product Management Haag GmbH

*Albert Haag and Laura Haag*

Combined slides for the MCP-CE (Novi Sad) and CONFWS'18  
(Graz), September 2018

PMH stands for Product Management Haag GmbH

Mass customization is about personalized products like T-shirts and cars. We have combined the slides of the two related presentations that were held within a week of each other.



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# QUASI-FINITE DOMAINS

## DEALING WITH THE INFINITE IN MASS CUSTOMIZATION

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- ★ *Very large tables (via compression)*
- ★ *Very fast evaluation of compressed form*
- ★ *vBase18™ Variant Management System*
- ★ *Substantially enhance legacy configurators (e.g. SAP VC)*
- ★ *Mass Customization (MC) is a natural application*

★ Leitmotiv: 85% of a product model might be pure tables

## Premises Concerning MC:

- Many mass customizable products can be defined by their variants
- Compression can handle the combinatorial explosion of variants

★ Simple compression to "c-tuples" already goes a long way

# Mass Customization (MC)

○ MC = mass production + individualization



**Ford Model-T  
1909**

One color  
"Black"

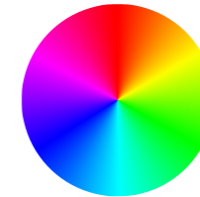


**Porsche 911  
1989**

Small list of  
colors

**BMW  
2029?**

Any RGB color  
16777216 colors



Picture by ModelTMitch - Own work, CC BY-SA 4.0, [Wikipedia link](#)

5  PMH

Quote attributed to Henry Ford (1909): "A customer can have a car painted any color he wants as long as it's black"

In 1909 mass production was the innovation more important than the individualization then available through traditional artisans

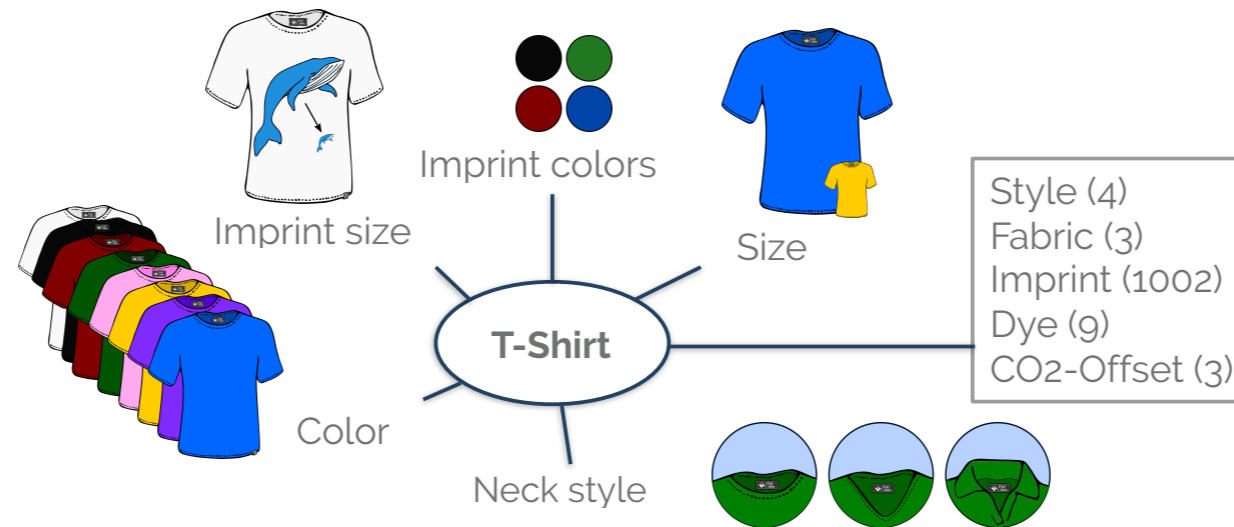
# Key Idea of Product Variants

- One generic product
- Variants distinguished by finite set of additional descriptive properties
- Simple example: felt pens mass produced in three colors
  - ▶ Product data and bill of materials maintained once
  - ▶ One descriptive property, *Color*, distinguishes variants



# MCT-Shirt - More than 270 Million Variants

10 properties, 1044 features, > 270 million combinations



- ★ Number of variants increases exponentially with choices
- ★ But not the complexity

MC T-shirt is the generic product

# Simple T-Shirt – Eleven Variants in a Table



Sizes M; L      Sizes S; M; L

Two "vintage" imprints

*Variant Table for Simple T-Shirt*

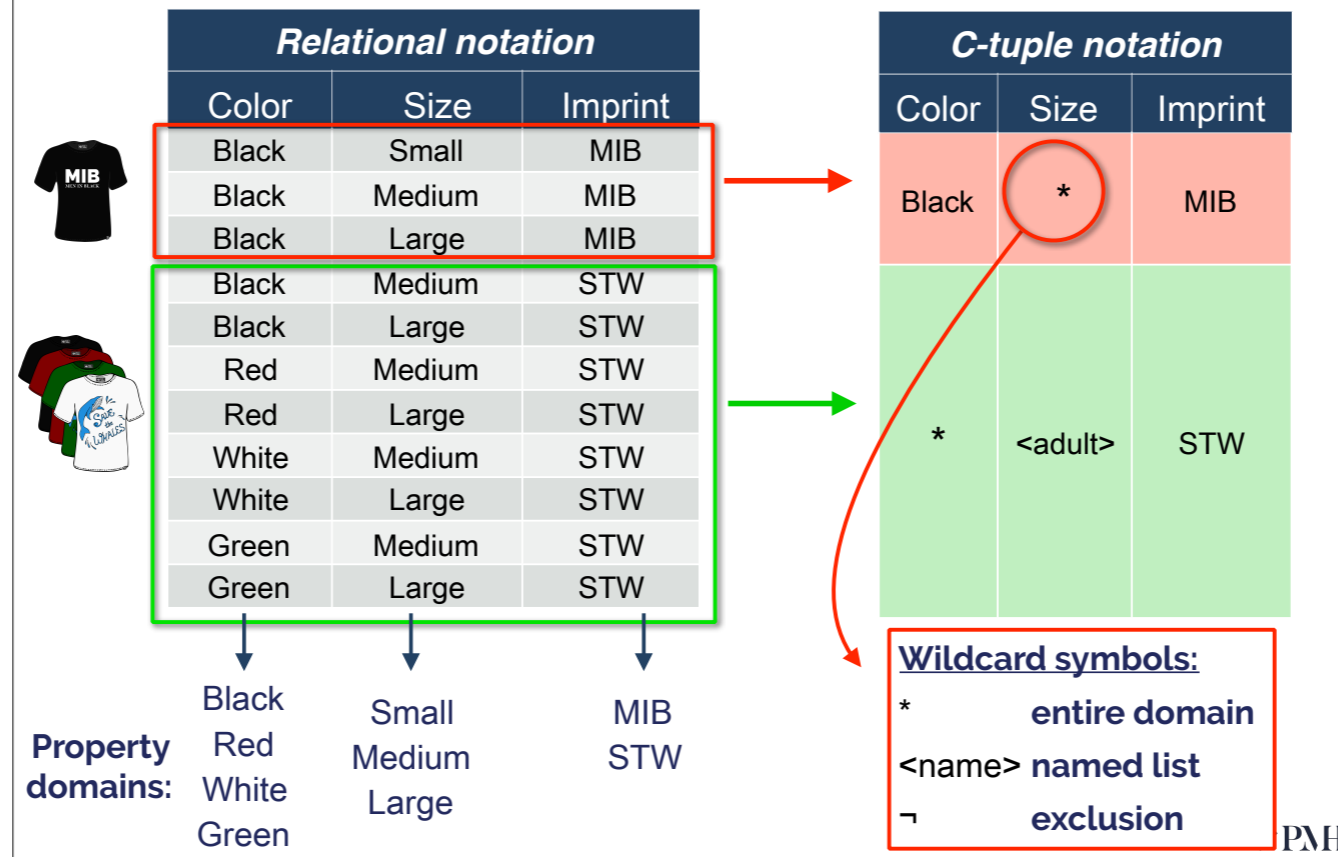
Color	Size	Imprint
Black	Small	MIB (Men in Black)
Black	Medium	MIB
Black	Large	MIB
Black	Medium	STW (Save the Whales)
Black	Large	STW
Red	Medium	STW
Red	Large	STW
White	Medium	STW
White	Large	STW
Green	Medium	STW
Green	Large	STW

★ Variant tables define legal combinations (function both as constraints and database tables)

Our terminology: product property: the "observable"; product feature is a value assignment to a property



# A C-Tuple Expresses Multiple Combinations



The first c-tuple with reddish background is interpreted as “black T-shirts come in any size with imprint ‘MIB’”. The second c-tuple with greenish background is interpreted as “T-shirts with imprint ‘STW’ come in any <adult> size (meaning ‘Medium’ or ‘Large’ – that is ¬‘Small’ ) and in any color”

## Configuration related filtering queries of variant tables:

- Result set of valid variants
- Domain restrictions
- Local (constraint) propagation

The following slides illustrate these queries

# Filtering Query

<i>Relational notation</i>		
Color	Size	Imprint
Black	Small	MIB
Black	Medium	MIB
Black	Large	MIB
Black	Medium	STW
Black	Large	STW
Red	Medium	STW
Red	Large	STW
White	Medium	STW
White	Large	STW
Green	Medium	STW
Green	Large	STW

<i>Query c-tuple</i>		
Color	Size	Imprint
Red	*	*

Result set

```
SELECT * FROM Simple-T-shirt WHERE <Query c-tuple>
```

★ Query conditions are c-tuples

# Domain Restriction for Color

<i>Relational notation</i>		
Color	Size	Imprint
Black	Small	MIB
Black	Medium	MIB
Black	Large	MIB
Black	Medium	STW
Black	Large	STW
Red	Medium	STW
Red	Large	STW
White	Medium	STW
White	Large	STW
Green	Medium	STW
Green	Large	STW

<i>Query c-tuple</i>		
Color	Size	Imprint
Red	*	*

Black  
Red  
White  
Green

SELECT DISTINCT Color FROM Simple-T-shirt WHERE <Query c-tuple>

# Domain Restriction for Size

<i>Relational notation</i>		
Color	Size	Imprint
Black	Small	MIB
Black	Medium	MIB
Black	Large	MIB
Black	Medium	STW
Black	Large	STW
Red	Medium	STW
Red	Large	STW
White	Medium	STW
White	Large	STW
Green	Medium	STW
Green	Large	STW

<i>Query c-tuple</i>		
Color	Size	Imprint
Red	*	*

Small  
Medium  
Large

SELECT DISTINCT Size FROM Simple-T-shirt WHERE <Query c-tuple>

# Domain Restriction for Imprint

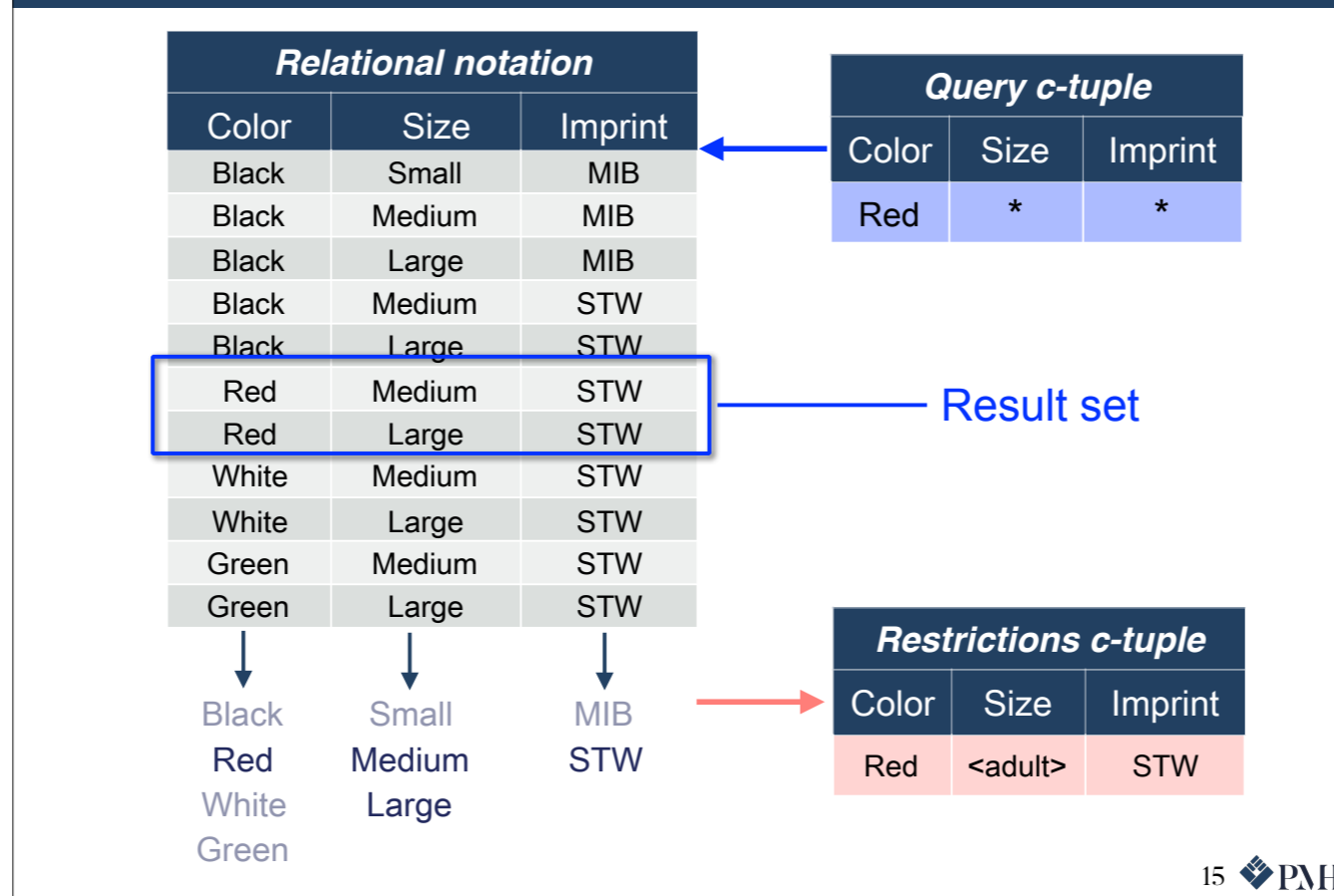
<i>Relational notation</i>		
Color	Size	Imprint
Black	Small	MIB
Black	Medium	MIB
Black	Large	MIB
Black	Medium	STW
Black	Large	STW
Red	Medium	STW
Red	Large	STW
White	Medium	STW
White	Large	STW
Green	Medium	STW
Green	Large	STW

<i>Query c-tuple</i>		
Color	Size	Imprint
Red	*	*

↓  
MIB  
STW

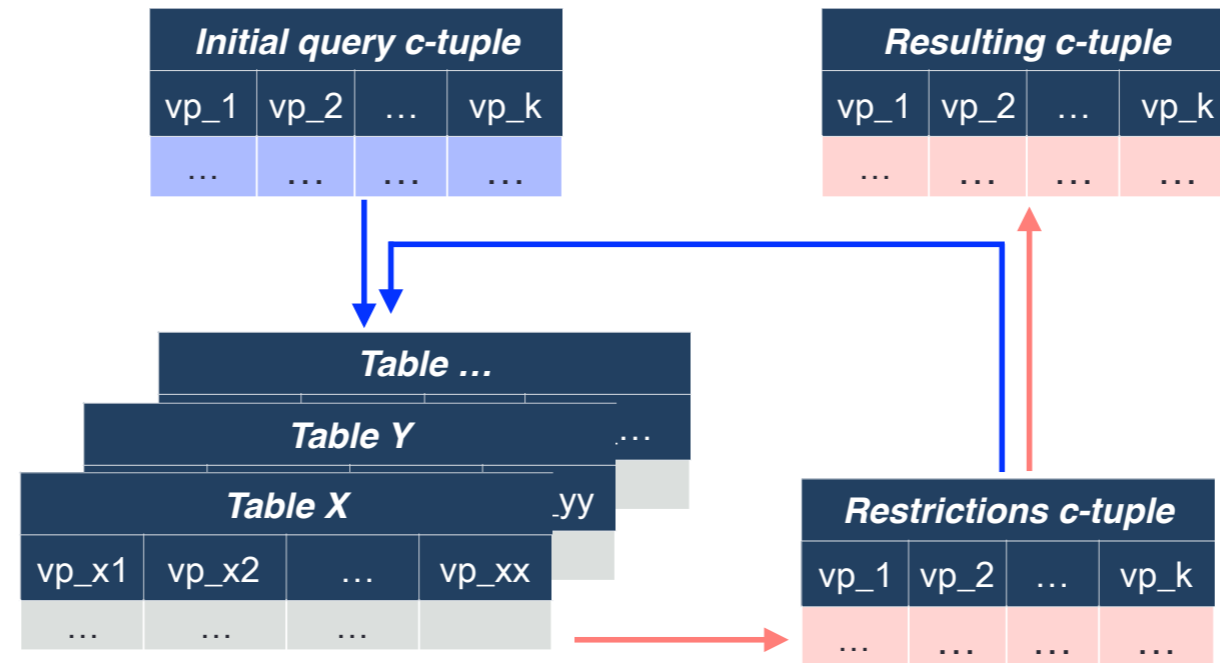
SELECT DISTINCT Imprint FROM Simple-T-shirt WHERE <Query c-tuple>

# Domain Restrictions as C-Tuple



One SELECT DISTINCT query for each of the columns can be combined to yield one resulting c-tuple representing the resulting restriction used in constraint propagation (arc-consistency)

# Local Constraint Propagation



★ Apply restrictions to all tables until no further restriction is possible (arc-consistency: result)

The query c-tuple is applied to all tables. Each ensuing restriction of the c-tuple is again applied to all tables, until no further restrictions occur. The c-tuple that allow no further restriction is the resulting overall domain restriction. This is a state of “arc-consistency”)



## Demo – MC T-shirt as two tables:

- 241 Million Sales variants
- 276 Million Manufacturing Variants

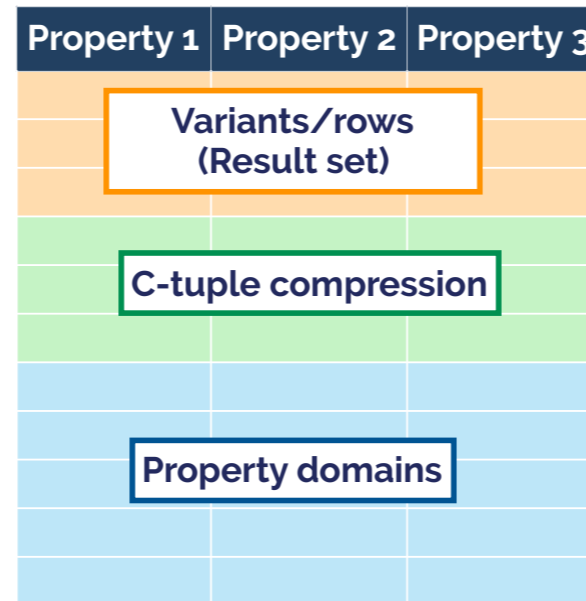
For purposes of demonstration, we have defined both a sales and a manufacturing model. Local propagation can be used to ensure consistency of the two models with each other.

## Four MC T-Shirt Constraints

- Imprint MIB: Black t-shirt, white imprint
- Imprint STW: Blue imprint, adult sizes
- Imprint color  $\neq$  T-shirt color (Sales)
- Fabric  $\leftrightarrow$  Color  $\leftrightarrow$  Dye (Manufacturing)

The first two constraints are common to both sales and manufacturing. Sales cares about imprints being clearly distinguishable. Manufacturing does not care about this, but cares about the dye needed for the T-shirt.

# Table View in Demo



# MC T-shirt model – overall variant table

View performance time after a query (selection/exclusion)

Complexity measure (approx. response time in microseconds) (for this example ~2 milliseconds)

Row 1 of 276514560    Ctuple 2 of 3    Complexity 1058    Time (ms) void

Table-3-Vintage-imprints.csv

Imprint	ImpCol	Size	Color	Style	Neck	Fabric	ImpSiz	CO2-Offset
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Baby	\$0.00
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Baby	\$0.99
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Baby	\$1.99
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Big	\$0.00
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Big	\$0.99
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Big	\$1.99
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Cute	\$0.00
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Cute	\$0.99
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	Cute	\$1.99
Imp_0002	Black	3T	Black	FullSleeve	Collar	Cotton	ExtraBig	\$0.00

View result set

Total number of rows

View/Select tuples

View/Select/Exclude property values (query)

Values in selected c-tuple are highlighted

# MC T-shirt sales model

Row 567123 of 241954560 Ctuple 3 of 7 Complexity 1071 Time (ms) void

Table-3-Vintage-imprints.csv Table-7-New-T-shirt-sales.csv Table-9-New-T-shirt-mfg.csv

ImpID	ImpColor	Color	Size	Style	Neck	Fabric	ImpSz	CO2-Offset
Imp_0004	Blue	White	3T	HalfSleeve	Round	Synthetic	Baby	\$0.99
Imp_0004	Blue	White	3T	HalfSleeve	Round	Synthetic	Baby	\$1.99
<<vintage>	Black	~(Black)	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	Blue	~(Blue)	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	Green	~(Green)	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	Red	~(Red)	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	White	~(White)	<*>	<*>	<*>	<*>	<*>	<*>
Imp_0002	Black	Black	3T	FullSleeve	Collar	Cotton	Baby	\$0.00
Imp_0003	Blue	Blue	4T	HalfSleeve	Round	Mixed	Big	\$0.99
Imp_0004	Green	Green	L	Hoodie	VNeck	Synthetic	Cute	\$1.99
Imp_0005	Red	Pink	M	NoSleeve			ExtraBig	
Imp_0006	White	Purple	S				Full	
Imp_0007		Red	XL				Medium	
Imp_0008		White	XS				Small	
Imp_0009		Yellow	XXL				Tiny	
Imp_0010								
Imp_0011								
Imp_0012								
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Imp_0030								
Imp_0031								
Imp_0032								
Imp_0033								
Imp_0034								
Imp_0035								

Result set scrolled to row 567123 of 241954560 sales variants; c-tuple viewer selected third of seven c-tuples; the values in this c-tuple are highlighted in the domains at the bottom; no selections or exclusions have been done.

# MC T-shirt manufacturing model

Row 123500677 of 276514560 Ctuple 3 of 19 Complexity 1092 Time (ms) void PMH M C P

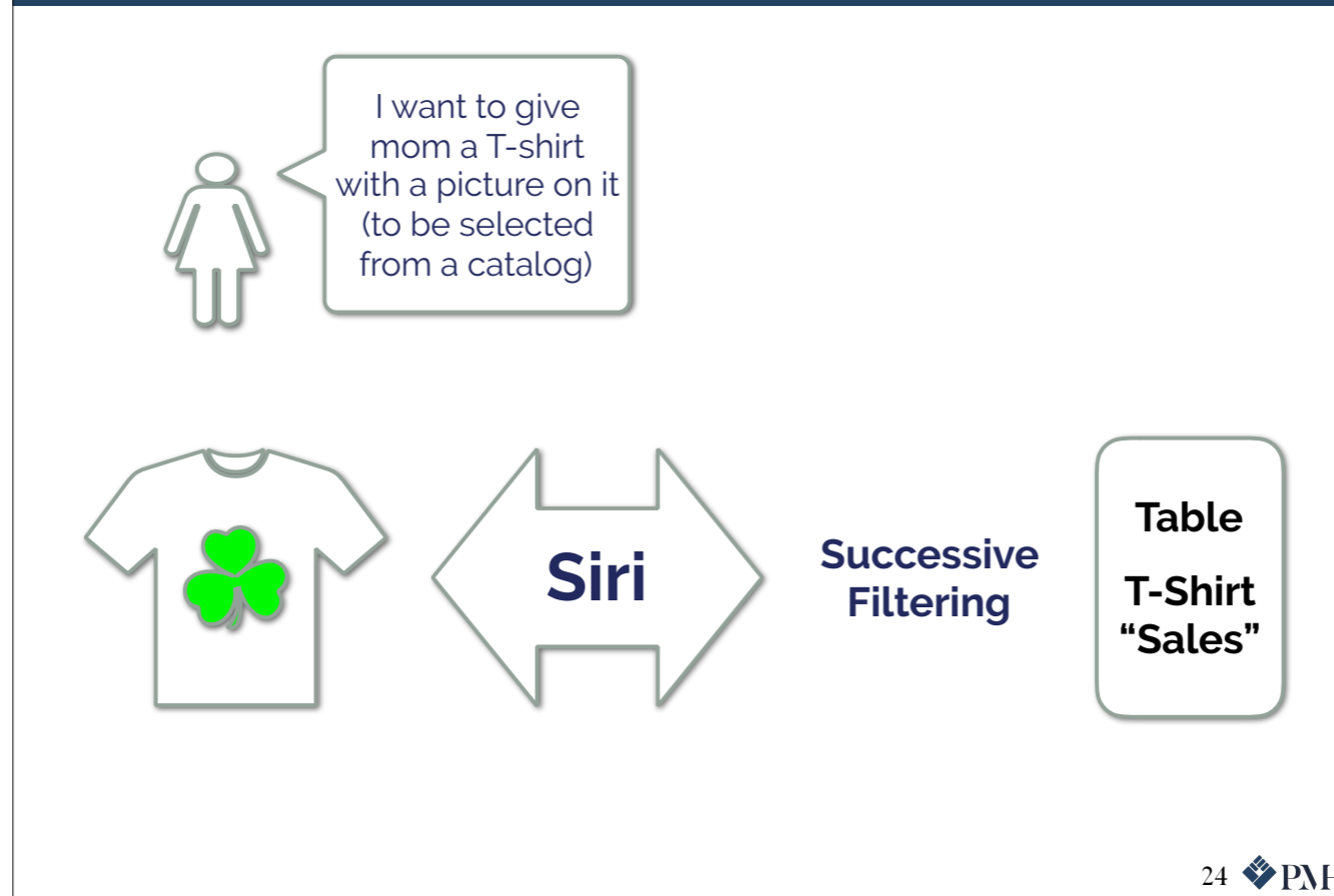
Impri	GrCD#	Color	Fabric	ImpCo	Size	Sleeve	Neck	ImpSz	CO2-Offset
Imp_0447	none	Blue	Mixed	Green	XL	NoSleeve	Mixed Collar	ExtraBig	\$1.99
Imp_0447	none	Blue	Mixed	Green	XL	NoSleeve	Collar	Fill	\$0.00
<<vintage>	GRCD#1	Green	Cotton	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	GRSD#2	Green	-(Cotton)	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	PICD#5	Pink	Cotton	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	PUSD#6	Pink	-(Cotton)	<*>	<*>	<*>	<*>	<*>	<*>
<<vintage>	PLUCD#3	Purple	Cotton	<*>	<*>	<*>	<*>	<*>	<*>
Imp_0002	GRCD#1	Black	Cotton	Black	3T	FullSleeve	Collar	Baby	\$0.00
Imp_0003	GRSD#2	Blue	Mixed	Blue	4T	HalfSleeve	Round	Big	\$0.99
Imp_0004	PICD#5	Green	Synthetic	Green	L	Hoodie	VNeck	Cute	\$1.99
Imp_0005	PISD#6	Pink		Red	M	NoSleeve		ExtraBig	
Imp_0006	PLUCD#3	Purple		White	S			Fill	
Imp_0007	PUSD#4	Red			XL			Medium	
Imp_0008	YCD#7	White			XS			Small	
Imp_0009	YSD#8	Yellow			XXL			Tiny	
Imp_001	none								
Imp_0010									
Imp_0011									
Imp_0012									
Imp_0013									
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Imp_0033									
Imp_0034									
Imp_0035									

Result set scrolled to row 123500677 of 276514560 manufacturing variants;  
 c-tuple viewer selected third of 29 c-tuples; the values in this c-tuple are highlighted in the domains at the bottom

Criticism of MC T-shirt with finite domains:

We should be able to deal with “additional values” for “Imprint”

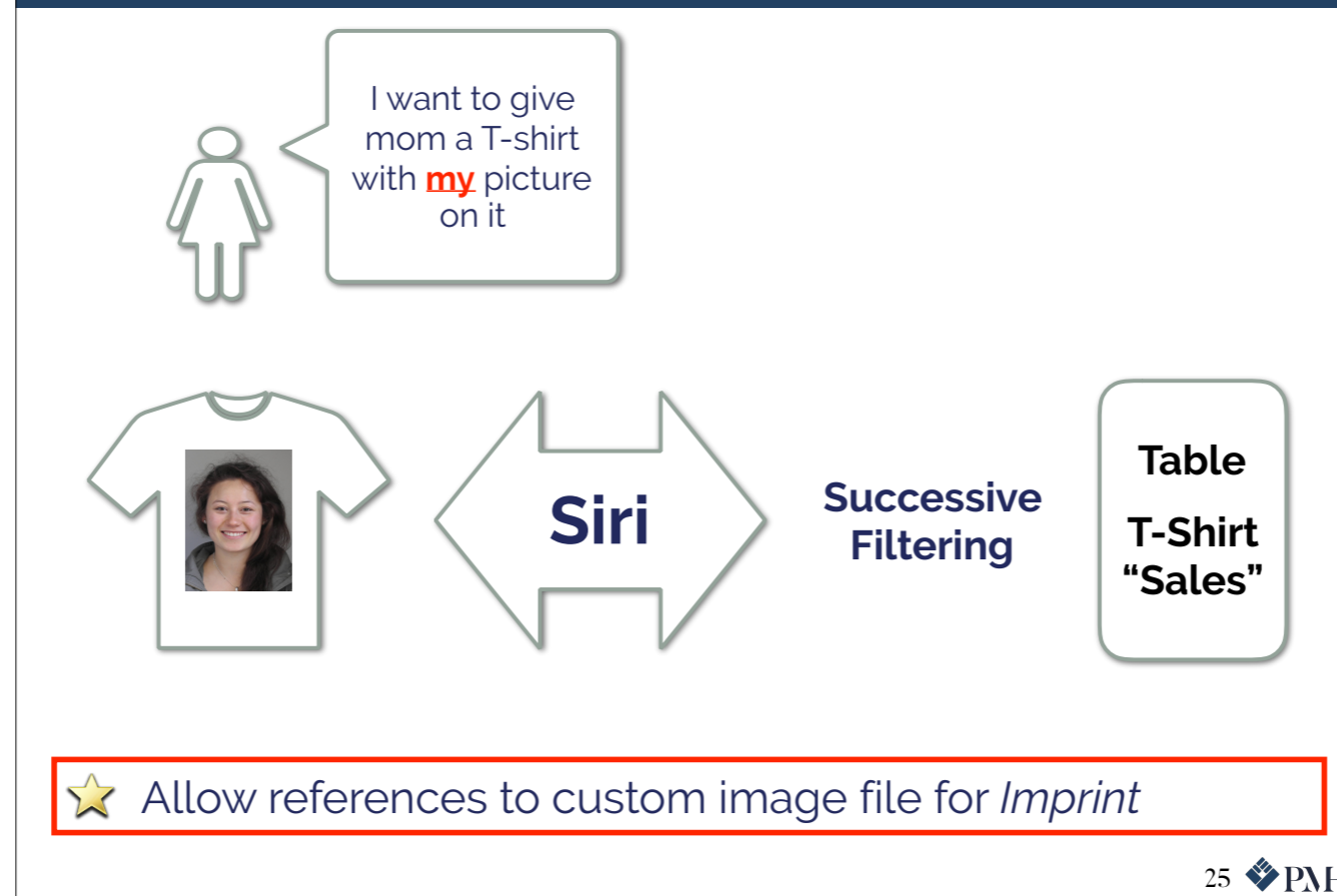
# Finite MC Scenario for Ordering a T-shirt



If Siri can order a Taxi, she can order a T-shirt. All it takes is finding a supplier, understanding their nine relevant T-shirt properties, and querying the sales variant table, which is in essence a “product catalog”



# Modern MC Scenario for Ordering a T-shirt



Here there is a slight additional complication. Siri needs to understand which filenames are legal. An illegal file name should lead to an appropriate error message, something we have not discussed here.

Idea: Introduce quasi-finite (QF)-  
symbols to encode infinite sets

Tables and domains remain finite in terms of  
symbols, but some symbols express infinite  
sets

Goals:

- Support compression as before
- Support constraint propagation/solving as before

# Allow Personal Image in Variant Tables

- Extend both sales and manufacturing table with the one c-tuple below
  - ▶ `<img-filename>` is a QF-symbol for the regular expression: `*.jpg | *.tif` to be allowed for Imprint
  - ▶ Column *Dye* only relevant for manufacturing table

<i>Imprint</i>	<i>ImpCol</i>	<i>Size</i>	<i>Color</i>	<i>Style</i>	<i>Neck</i>	<i>Fabric</i>	<i>ImpSiz</i>	<i>CO2-Offset</i>	<i>Dye</i>
<code>&lt;img-filename&gt;</code>	*	*	White	*	*	*	*	*	none

# Sample Interaction with QF-Symbols

Using QF-symbols for real-valued intervals

# QF-Symbols in Domain Restriction

Query for all small ("S") T-shirts

Size	ImpSize	Scale
S	Cute	[0.1, 0.2]
S	Big	[0.5, 0.6]
S	Fill	[0.7, 0.9]
M	Cute	[0.2, 0.3]
M	Big	[0.75, 0.9]
M	Fill	[1.0, 1.2]
L	Cute	[0.25, 0.4]
L	Big	[0.75, 0.9]
L	Fill	[1.3, 1.9]

Query c-tuple		
Size	ImpSiz	Scale
S	*	*

Restrictions c-tuple		
Size	ImpSize	Scale
S	*	[0.1, 0.2], [0.5, 0.6], [0.7, 0.9]

"Xnumeric"

Xnumeric datatype: an ordered set of normalized (i.e. non-overlapping) intervals, including singleton intervals to represent individual numbers

# Normalized QF-Symbols in Domain Restriction

Query: All "Cute" imprint sizes

Size	ImpSize	Scale
S	Cute	[0.1, 0.2]
S	Big	[0.5, 0.6]
S	Fill	[0.7, 0.9]
M	Cute	[0.2, 0.3]
M	Big	[0.75, 0.9]
M	Fill	[1.0, 1.2]
L	Cute	[0.25, 0.4]
L	Big	[0.75, 0.9]
L	Fill	[1.3, 1.9]

Query c-tuple		
Size	ImpSiz	Scale
*	Cute	*

Restrictions c-tuple		
Size	ImpSize	Scale
*	Cute	[0.1, 0.4]

"QF-interval"  
(xnumeric normalization)

[0.1, 0.2]  
[0.2, 0.3]  
[0.25, 0.4] } [0.1, 0.4]

Normalized xnumeric datatype: merge overlapping intervals to one interval

# QF-Symbols in Query and Condition

Query: Scale IN [0.6, 1.1]

Size	ImpSize	Scale
S	Cute	[0.1, 0.2]
S	Big	[0.5, 0.6]
S	Fill	[0.7, 0.9]
M	Cute	[0.2, 0.3]
M	Big	[0.75, 0.9]
M	Fill	[1.0, 1.2]
L	Cute	[0.25, 0.4]
L	Big	[0.75, 0.9]
L	Fill	[1.3, 1.9]

Query c-tuple		
Size	ImpSiz	Scale
*	*	[0.6, 1.1]

Restrictions c-tuple		
Size	ImpSize	Scale
*	Big;Fill	0.6, [0.7, 0.9], [1.0, 1.1]

(xnumeric intersection with normalization)

# Summary: Necessary QF-Operations

- We need following operations given two QF-symbols for the same product property
  - ▶ **Union** (normalization)
  - ▶ **Intersection** (specialization)
  - ▶ **Negation** (good to have, needed in VDD construction)
    - Implies exclusion sets (see paper))

★ Any set of symbols that satisfy these requirements can be used for QF-symbols, e.g. "Rectangles" etc.

★ Generalizes to a "specialization relation"



# Specialization Relation

A partial ordering on a set of symbols (QF-symbols or values) such that:

- *Constraint processing* need not consider an otherwise valid symbol assignment to a product property in the presence of a more special one (*procedural-subsumption property*).
- A symbol assignment is logically implied by any of its specializations (*semantic-compatibility property*).
- Negation inverts specialization (*symmetry-under-negation property*).

 [See papers](#)

## References:

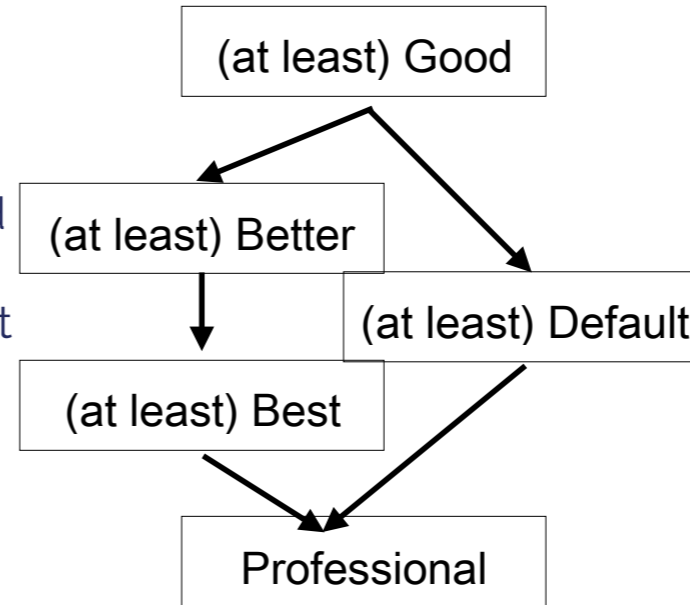
- Albert Haag and Laura Haag, 'Empowering the use of variant tables in mass customization', in Proceedings of the MCP-CE 2018 conference, Novi Sad, Serbia, September 19-21, 2018., pp. 180-189, (2018).
- Albert Haag, 'Quasi-finite domains: relaxing finiteness of domains and mass customization', in Proceedings of the 20th International Configuration Workshop, Graz, Austria, September 27-28, 2018., pp. 77-84, (2018).

# Examples of Specialization

- An additional value for Property *Imprint*: specializes `<img-filename>` if it matches the regular expression; otherwise it signals a contradiction
  - ▶ “my-image.jpg” is a specialization
  - ▶ “blueberry” is an illegal assignment
- If the two assignments **Scale IN [0.6, 1.1]** and **Scale IN [1.0, 1.2]** need to be considered simultaneously, they must be replaced by their common specialization **Scale IN [1.0, 1.1]**
- Next slide illustrates specialization for an additional property (image) *Resolution*, with a finite domain arranged in a specialization relation

# Image Resolution — Finite Specialization Relation

- If the two assignments  
Resolution = 'Better' and  
Resolution = 'Default' need  
to be considered  
simultaneously, they must  
be replaced by their  
common specialization  
Resolution = 'Professional'



★ Example of finite specialization relation



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- Web: <http://product-management-haag.de>
- [www.vbase18.com](http://www.vbase18.com)

ANY QUESTIONS?

# THANK YOU!

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We have dedicated the vBase18-engine to our son and brother Olaf "in memoriam". He was in this at the start and we sorely miss him.